

## MATH 3451 Homework Assignment 4

**Instructions:** Solve and turn in all of the assigned problems, taken from our textbook. Problems marked with a \* must be done by graduate students, and may be attempted by undergraduates for extra credit.

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Due on Thursday, October 17th at the beginning of class.

Section 1.6 (page 43): 2, 4(a,c), 6 (for 4(a), a set  $T$  of sequences is ‘closed’ if the limit of a convergent sequence in  $T$  must also be in  $T$ .)

- Prove that if  $\mu > 5$ , then  $S^{-1}$  is continuous, where  $S$  is the symbolic coding map from  $\Lambda$  to  $\Omega_2 = \{0, 1\}^{\mathbb{N}}$  from class. (Hint: you can use problems from the last homework assignment!)
- If  $\mu > 2 + \sqrt{5}$ , how many points of least period 4 does the function  $f_\mu(x) = \mu x(1 - x)$  have? (If you’re doing this by using sequences in  $\Omega_2$ , you need to explain why they have the desired properties after being transferred to  $\Lambda$ .)