

Name:		
Class time: (circle the one for your class)	11.90 12.00	1:00 - 2:00
Instructions: This test should have 12 pa 100 points. Please answer each question as a work unless otherwise indicated. You may exam. (Approved: non-graphing, non-progra	completely as possibuse an approved ca	ole, and show al liculator for this

1. (6 pts.) Compute the derivative of $f(x)=\frac{5}{3-2x}$ at x=-1 by using the LIMIT DEFINITION of the derivative.

2. (6 pts.) Find the absolute/global maximum and minimum of the function $f(x)=2x^3-3x^2-12x+1$ on the domain [-2,0].

3. (5 pts.) Use logarithmic differentiation to find the derivative of $f(x)=\frac{(3x+1)^{10}e^{\sqrt{x}}}{(\sin x)^5}.$

 $\bf 4.~(15~pts.;~5~pts.~each)$ Find the derivatives of the following functions. You do NOT need to simplify your answers.

(a)
$$h(x) = \sin x \sin(x^2) \sin(x^3)$$

(b)
$$g(x) = \frac{3^x + 4^{-x}}{4^x - 3^{-x}}$$

(c)
$$f(x) = \sqrt{\arctan x} + \arctan \sqrt{x}$$

5. (8 pts.) Find the intervals where the function $f(x) = 4x - \tan x$ is increasing and decreasing within the domain $[0, 2\pi]$.

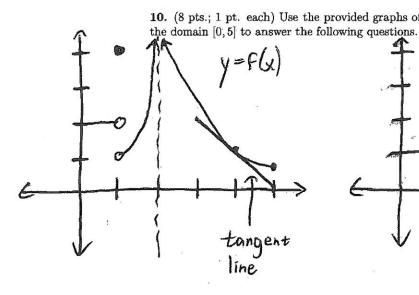
6. (8 pts.) Find all horizontal and vertical asymptotes of $f(x) = \frac{x^{\frac{4}{3}} + 2}{x^{\frac{1}{3}} - x^{\frac{4}{3}}}$.

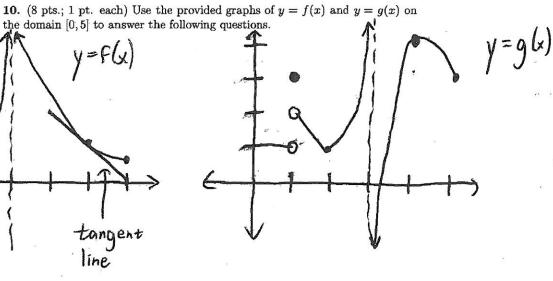
7. (15 pts.) A spotlight on the ground shines on a wall 12 m away. A man 2 m tall walks from the spotlight towards the wall at a rate of 3 m/s. How fast is the length of his shadow on the building changing when he is 2 feet from the spotlight?

8. (6 pts.) Use linear approximation to approximate $\sqrt[3]{8.1}$.

9

& (15 pts.) A cylinder has surface area 24π square feet. What is the maximum possible volume of such a cylinder? (Hint: the surface area of a cylinder is $2\pi r^2 + 2\pi rh$.)





- (a) For what values of x is f(x) discontinuous?
- (b) For what values of x is g(x) nondifferentiable?

(c) Find
$$\lim_{x\to 1^-} (f(x) + g(x))$$
.

(d) Find
$$\lim_{x\to 1^+} (f(x) + g(x))$$
.

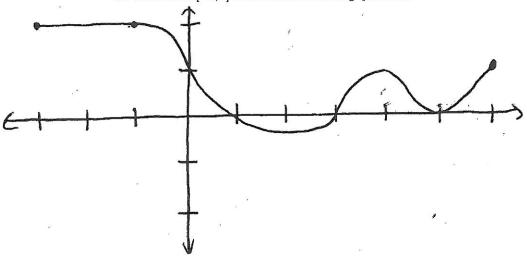
(e) Is
$$f(x) + g(x)$$
 continuous at $x = 1$?

(f) Find the derivative of
$$f(x) - g(x)$$
 at $x = 4$.

(g) Find the derivative of
$$f(x)g(x)$$
 at $x=4$. (h) Find the derivative of $f(g(x))$ at $x=4$.

(h) Find the derivative of
$$f(g(x))$$
 at $x = 4$.

11. (6 pts.; 1 pt. each) Use the provided graph of y = f'(x) (NOT y = f(x)!!!) on the domain [-3, 6] to answer the following questions.



- (a) On what intervals is f(x) decreasing?
- (b) At what x-values does f(x) have local extrema?
- (c) On what intervals is f(x) concave up?
- (d) At what x-values does f(x) have inflection points?
- (e) What is f(-1) f(-3)?
- (f) In your own words, why isn't it possible to draw an accurate graph of y = f(x), even with exact information about all values of f'(x)?

12. (6 pts.) Show that the function $f(x) = x^5 + x^2 + x + 1$ has some tangent line with slope 3. You do NOT need to solve for the x-value where this tangent line occurs. (Hint: you can do this with either the Intermediate Value Theorem OR the Mean Value Theorem)