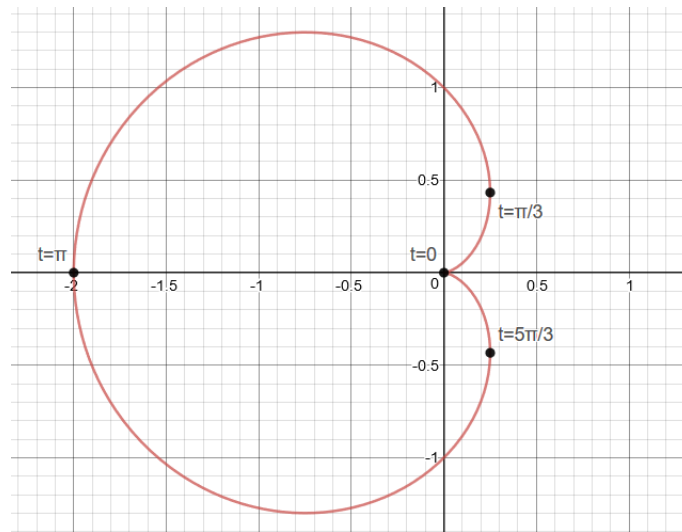


Friday Week 1  
Calculus III

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Above is a graph of a cardioid, parametrized by

$$\begin{aligned}x(t) &= (1 - \cos t) \cos t \\y(t) &= (1 - \cos t) \sin t \\0 \leq t &\leq 2\pi\end{aligned}$$

- (a) Use the graph to determine when  $x(t)$  is increasing/decreasing, and when  $y(t)$  positive/negative.
- (b) Give an expression for the area enclosed by the cardioid (but do not integrate). You may make use of symmetry.

Consider the parametric curve

$$\begin{aligned}x(t) &= t^3 - 4t \\y(t) &= t^2 \\0 &\leq t \leq 2\end{aligned}$$

(a) Without graphing, determine when  $x(t)$  is increasing/decreasing, and when  $y(t)$  positive/negative.

(b) Give an expression for the area enclosed by the curve and the  $y$ -axis (but do not integrate).