MATH 3851 Homework Assignment 7 (due Monday, March 1st)

Textbook problems:

Section 39: (p. 125-126) 5 Section 45: (p. 149) 2(a,c) Section 49: (p. 160-163) 1(c,f), 2(c) Section 52: (p. 170-171) 1(b,c), 2(a,b), 5

Extra problems:

• Give an example of a contour Γ (with parametrization) for which $\int_{\Gamma} \frac{1}{z} dz = -3\pi i$.

• Give a deformation function which shows that Γ_0 is continuously deformable to Γ_1 in \mathbb{C} , where Γ_0 is the circle $\{z : |z+1| = 4\}$ traversed in the counterclockwise direction, and Γ_1 is the circle $\{z : |z-1| = 2\}$ traversed in the counterclockwise direction. (HINT: The easiest way is probably to shrink the radius from 4 to 2 first (say from s = 0 to $s = \frac{1}{2}$), and then to move the circle from being centered at -1 to centered at 1 (say from $s = \frac{1}{2}$ to s = 1.)